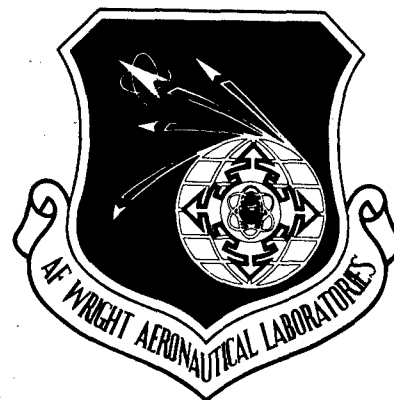


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EFFECT OF FREQUENCY ON  
FATIGUE CRACK GROWTH RATE  
OF INCONEL 718 AT HIGH  
TEMPERATURE



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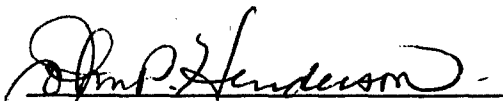


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# TABLE OF CONTENTS

<u>SECTION</u>		<u>PAGE</u>
1	INTRODUCTION	1
2	EXPERIMENTAL TECHNIQUE	4
2.1	OVERVIEW	4
2.2	SPECIMEN GEOMETRY AND MATERIAL	5
2.3	TEST CONDITIONS	
2.4	TEST SYSTEM	8
2.5	MEASUREMENT OF CRACK LENGTH	8
2.5.1	<u>Compliance Method</u>	10
2.5.2	<u>Electric Potential Method</u>	10
2.5.3	<u>Correction for Apparent Changes in Crack Length</u>	11
2.6	TEST PROCEDURE	12
2.7	GROWTH RATE MONITORING	12
3	RESULTS AND DISCUSSION	15
3.1	GROWTH RATE-FREQUENCY PLOTS AT $R = 0.1$	15
3.1.1	<u>Fully Time-Dependent Growth</u>	19
3.1.2	<u>Environmentally Enhanced Cycle-Dependent (Mixed) Growth</u>	19
3.1.3	<u>Fully Cycle-Dependent Growth</u>	20
3.2	EFFECT OF $K_{max}$ ON FCGR-FREQUENCY PLOTS AT A GIVEN $R$ ( $R = 0.1$ )	21
3.3	EFFECT OF $R$ ON GROWTH RATE-FREQUENCY PLOTS AT $K_{max} = 40 \text{ MPa} \cdot \text{m}^{1/2}$	22

## TABLE OF CONTENTS (Concluded)

<u>SECTION</u>	<u>PAGE</u>
3.4 TRANSITION FREQUENCIES	24
3.5 MICRO-MECHANISMS OF CRACK GROWTH	24
3.6 MECHANISMS OF DAMAGE IN FULLY TIME-DEPENDENT REGIME	26
3.7 MODELING THE GROWTH BEHAVIOR	27
3.7.1 <u>Prediction of Growth Rates in the Fully Time-Dependent Region</u>	28
3.7.2 <u>Prediction of Growth Rates in the Mixed Region</u>	30
3.7.3 <u>Prediction of Growth Rates in Fully Cycle-Dependent Region</u>	31
4 CONCLUSIONS	33
REFERENCES	34

## LIST OF ILLUSTRATIONS

<u>FIGURE</u>		<u>PAGE</u>
1	The C(T) Specimen Modified for DC Potential and Displacement Measurements.	6
2	Fractured Specimens of Inconel 718 Showing Different Cracking Regions Corresponding to Test Under Different Conditions.	13
3	Typical $a$ vs $N$ Experimental Data with the Fitted Linear Regression Line.	16
4	Fatigue Crack Growth Rate ( $da/dN$ ) for Inconel 718 as a Function of Frequency at $R = 0.1$ , Temperature = $650^{\circ}\text{C}$ at Two Different $K_{\max}$ Values, 27.8 and $40 \text{ MPa}\cdot\text{m}^{1/2}$ . Also Data in Vacuum at 1 Hz [17] and Room Temperature Air Data are Given.	17
5	Time Rate of Crack Growth, ( $da/dt$ ) for Inconel 718 as a Function of Frequency at $K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$ , $R = 0.1$ , and Temperature = $650^{\circ}\text{C}$ .	18
6	Fatigue Crack Growth Rate, ( $da/dN$ ) for Inconel 718 as a Function of Frequency at $K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$ and Temperature = $650^{\circ}\text{C}$ for Three Different $R$ Values, 0.1, 0.5, and 0.8. Also 1 Hz Vacuum Data Points [17] and Room Temperature Data are Given for $R = 0.1$ and 0.5.	23
7	Scanning Electron Fractographs of Typical Fracture Surfaces for (a) Cycle-Dependent (10 Hz) Region, (b) Mixed (0.5 Hz) Region, and (c) Time-Dependent (0.002 Hz) Region. These Tests were Conducted at $650^{\circ}\text{C}$ , $R = 0.1$ , and $K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$ .	25
8	FCGR for Inconel 718 at Room Temperature ( $38^{\circ}\text{C}$ ) and 1 Hz as a Function of $(1-R)$ for $K_{\max} = 27.8$ and $40 \text{ MPa}\cdot\text{m}^{1/2}$ .	32

## LIST OF TABLES

<u>TABLE</u>		<u>PAGE</u>
1	CHEMICAL COMPOSITION BY WEIGHT AND HEAT TREATMENT FOR INCONEL 718	7



## SECTION 1

### INTRODUCTION

Turbine engine disks of nickel-base superalloys are subjected to cyclic stresses and thermal transients at elevated temperatures as a result of throttle excursions and thermal gradients [1]. These operations produce loading patterns that cover a range of frequencies, amplitudes, and waveshapes. The Air Force has recently introduced damage tolerance requirements for critical structural components such as turbine disks. It is important, therefore, to be able to predict the growth rate of fatigue cracks in disk materials under the appropriate loading and temperature histories experienced in engines. This can be accomplished through a systematic study of the influence of the individual loading variables and the possible interactions among them. In the development of any model, the governing microstructural mechanisms should provide guidance.

Rates and micro-mechanisms of crack growth in nickel-base superalloys are, in general, a function of the maximum stress intensity factor ( $K_{\max}$ ), temperature ( $T$ ), frequency ( $f$ ), stress ratio ( $R$ ), hold-time ( $t_H$ ), waveshape, as well as material and microstructure. If all the variables except  $K_{\max}$  are held constant, then the crack growth rate for most nickel-base superalloys such as Inconel 718 can be correlated with stress intensity factor as the governing parameter [2,3,4,5,6,7,8,9]. The other variables can then be used as modifying parameters in

modeling the behavior. To fully characterize fatigue crack growth rate (FCGR) as a function of one of the above variables, experiments can be conducted with other variables held constant throughout the test.

Modeling the FCGR behavior and interpreting the changes in micro-mechanisms of crack growth reduce to determining the explicit relationships of the independent variables in the expressions

$$da/dN = F_1(K_{max}, T, f, R) \quad (1)$$

$$\text{micro-mechanism of growth} = F_2(K_{max}, T, f, R) \quad (2)$$

In this paper, rates and micro-mechanisms of fatigue crack growth were studied as a function of two independent variables, frequency and  $R$ , in Equations 1 and 2 at  $T = 650^\circ\text{C}$ .

In air and vacuum, under low cycle fatigue conditions, crack growth rate as a function of frequency has been studied in detail by Solomon [10,11]. He identified the existence of three major frequency regimes in air. Under  $K$ -controlled LEFM conditions [12], the present author obtained similar results for Inconel 718 at  $650^\circ\text{C}$ . The results from this investigation and others [6,7] show that for a given  $K_{max}$ , FCGR decreases with increasing frequency. At higher frequencies, the growth rate approaches a constant value. It has also been observed that the

crack growth mechanism changes from intergranular to transgranular with increasing frequency.

## SECTION 2

### EXPERIMENTAL TECHNIQUE

#### 2.1 OVERVIEW

Systematic studies of fatigue crack growth as a function of test variables generally involves large numbers of constant load tests leading to scatter from specimen to specimen. In this investigation, the growth rates were obtained at two  $K_{\max}$  values for three R values in a range of five decades of frequencies using only two specimens to obtain the necessary experimental information for the investigation. To minimize possible closure effects on crack growth, relatively high stress intensity factors which lie in the mid-power law region of the FCGR versus  $K_{\max}$  curves were selected. In designing the experiments, the fact that the growth rate could be correlated with a power law function of  $K_{\max}$  was taken into consideration. The power-law FCGR function has been reported in literature and also observed in this laboratory under various frequencies and hold-time conditions [13]. The method of testing was different from that typically used, where the tests are conducted under constant loading conditions by using a specimen for each test condition. This testing approach facilitated the study of crack growth behavior over a range of five decades of frequencies.

## 2.2 SPECIMEN GEOMETRY AND MATERIAL

A series of FCGR tests were conducted on Inconel 718 nickel-base superalloy. Tests were conducted using standard (ASTM E647) [14] C(T) specimens having a width,  $W$  of 40 mm and a thickness,  $B$  of 10 mm. To make the d.c. potential measurement of crack length, two Inconel 718 metal rods were welded to the C(T) specimen for the connection of the d.c. current supply. Leads for the d.c. electric potential measurements were spot-welded across the crack mouth. A diagram of the C(T) specimen with d.c. current rods is shown in Figure 1. Note also the location of the two holes which accepted the ends of the quartz rods attached to the extensometer used for compliance measurements.

All specimens were fabricated from the same heat of material. The heat treatment and composition of the IN718 material are shown in Table 1.

## 2.3 TEST CONDITIONS

All crack growth tests were conducted under constant stress intensity conditions. Two  $K_{\max}$  values of 27.8 and 40  $\text{MPa}\cdot\text{m}^{1/2}$  were chosen to define the levels. Both these values lie in the mid-power law region of FCGR vs  $K_{\max}$  curve. The tests were conducted over frequencies chosen from the range of 0.001 to 50 Hz and at a temperature of 650°C. Three different  $R$  ratios,

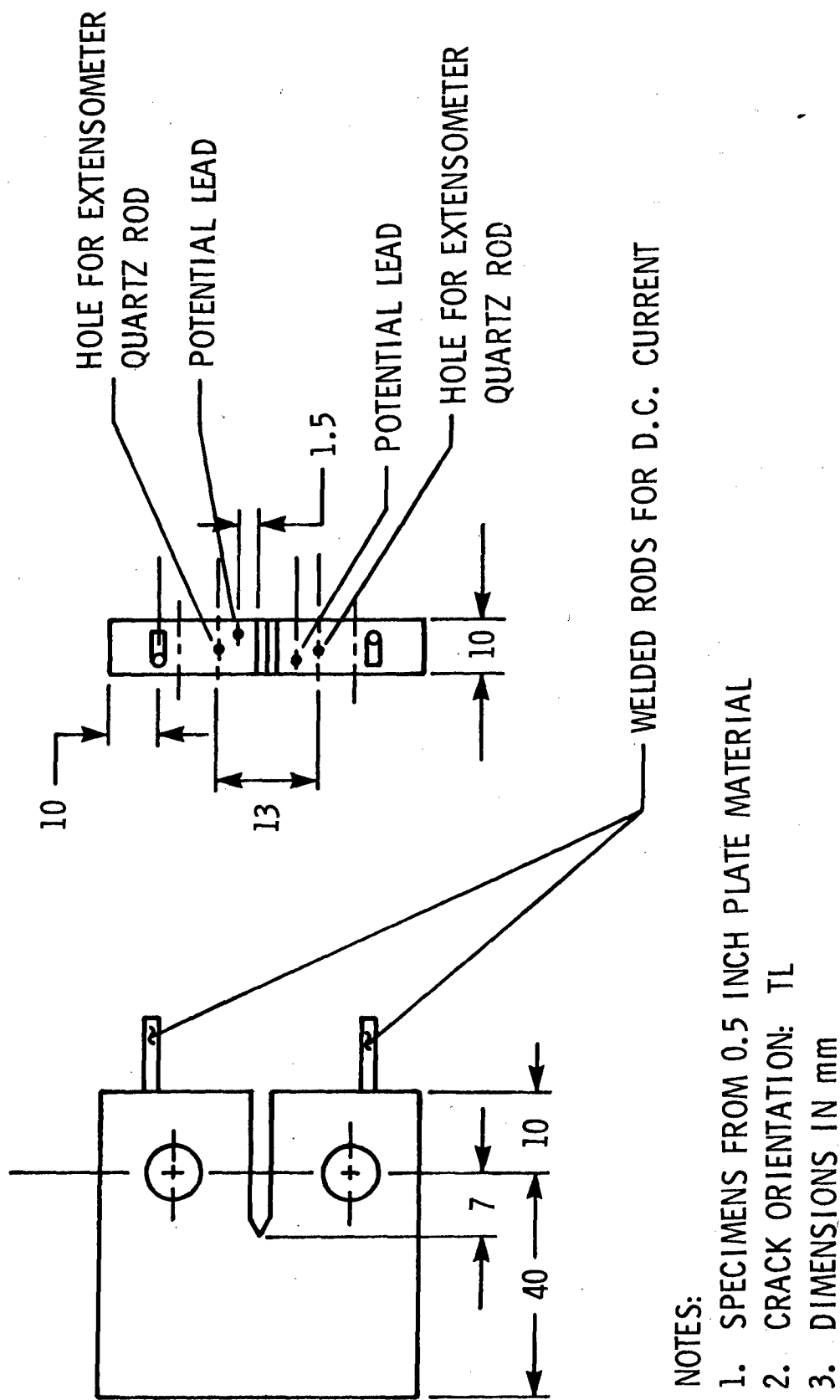


Figure 1. The C(T) Specimen Modified for DC Potential and Displacement Measurements.

TABLE 1

CHEMICAL COMPOSITION BY WEIGHT AND HEAT  
TREATMENT FOR INCONEL 718

Ni	50-55	Cr	17-21
Fe	BAL.	Nb+Ta	4.75-5.5
Mo	2.8-3.3	Ti	0.65-1.15
Al	0.2-0.8	Co	<1.0
C	<0.08	Mn	<0.35
Si	<0.35	Cu	<0.30
Ph	<0.015	S	<0.015
B	<0.006		

## HEAT TREATMENT

- Step 1: Anneal at 968°C (1775°F) for 1 Hr., Air Cool to 718°C (1325°F).
- Step 2: Age Harden at 718°C (1325°F) for 8 Hrs., Then Furnace Cool at 56°C/Hr. (100°F/Hr.) to 621°C (1150°F).
- Step 3: Age Harden at 621°C (1150°F) for an Additional 8 Hrs.
- Step 4: Air Cool to Room Temperature.

0.1, 0.5, and 0.8 were used in these experiments. A triangular loading waveform was utilized in all of the tests.

Specimens were precracked at 650°C to a crack length given by the ASTM E647 Standard ( $a = 10$  mm) by applying a constant stress intensity that was less than the stress intensities used in the experiments.

## 2.4 TEST SYSTEM

An automated test system based on a microcomputer was employed in conducting these experiments. An electro-hydraulic servo-controlled test station with a 25 KN load cell was used to apply loading during the course of these tests. The microcomputer was used in real-time for feedback control of the test parameters and also to acquire and reduce data. The specimen was heated with a resistance furnace, and the temperature at a point on the specimen was controlled at  $650 \pm 2^\circ\text{C}$ . The temperature variation along the crack path was noted to be less than  $10^\circ\text{C}$ .

## 2.5 MEASUREMENT OF CRACK LENGTH

Crack length was measured in the range of frequencies between  $10^2$  and  $10^{-3}$  Hz, using a hybrid crack measuring system. In this system, crack lengths were measured by both compliance and d.c. electric potential techniques. During testing,  $K_{\max}$



control was accomplished in different frequency ranges using one of the two techniques. Due to the inability of the extensometer to track the displacement correctly, the d.c. electric potential technique was used exclusively at high frequencies ( $f > 1.0$  Hz). For lower frequencies ( $f \leq 1.0$  Hz), controlling crack lengths were determined by the compliance technique. For the  $f \leq 1.0$  Hz case, the d.c. electric potential crack length data were also collected for later evaluation of their accuracy and long term stability under the effect of environment at very low frequencies. Acquisition of load and displacement (compliance) data from the specimen to the microcomputer was accomplished using a digital oscilloscope. Electric potential data acquisition from the test machine to the microcomputer was performed utilizing a digital voltmeter.

The crack length was estimated at periodic cycle intervals chosen by the operator. The cycle interval was chosen to give a crack length increment less than 0.025 mm. After the crack length is determined using the stress intensity relationship given in ASTM E647 [14], the new load that is necessary to keep the  $K_{\max}$  constant is determined by the computer software to within  $\pm 0.1\%$ . This computed load was then set up at the function generator through the IEEE-488 interface.

### 2.5.1 Compliance Method

During the test, crack length was determined indirectly from compliance measurements using displacement data obtained with a high temperature extensometer having quartz extension rods. With these quartz rods, the extensometer was maintained at ambient temperature since it was kept outside the furnace. Displacement and load data obtained simultaneously in digital form with the oscilloscope were transferred to the computer through an IEEE-488 interface bus. A straight line was fitted to a selected set of data chosen by a specified load window, using a least-squares error minimization procedure. Compliance that was obtained from the fitted straight line was converted to crack length using a relationship obtained by Saxena and Hudak [15] given in Equation 3, where C is the compliance, E is the modulus, B is the thickness of the specimen, and  $b = a/W$ .

$$CEB = (1+0.25/b) [(1+b)/(1-b)]^2 \{1.61369+12.6778b -14.2311b^2-16.6102b^3+35.0499b^4-14.4943b^5\}. \quad (3)$$

### 2.5.2 Electric Potential Method

Using the d.c. electric potential technique, crack length was determined at higher frequencies by measuring the potential across the crack tip at a constant d.c. current of 10 A. The constant current was generated by a stable power supply while the potential was measured by the voltmeter. Both

the power supply and the voltmeter were attached to the computer through the IEEE-488 bus. Using these instruments and the developed software, data were acquired and test conditions were controlled. To eliminate the thermal e.m.f., the potential data were also obtained at zero current. The electric potential data were acquired a given number of times at the upper one-third of a predefined number of successive cycles. The thermal e.m.f. adjusted average value of the potential was then converted to a crack length using an experimentally determined calibration curve.

### 2.5.3 Correction for Apparent Changes in Crack Length

It was observed that whenever  $f$ ,  $K_{\max}$ , or  $R$  was changed, the crack length estimated by the compliance method changed. The change in compliance estimated crack length occurred immediately after the change in external parameters and was not associated with any real change in crack length. Rather than continuing to use the newly estimated crack length that was established after the change, a procedure was developed to ensure continuity in crack length before and after the change in loading parameters. In essence, the procedure involved modifying the apparent elastic modulus after each change in loading parameters, so that the crack length before and after the change remained the same based on Equation 3.

## 2.6 TEST PROCEDURE

Using a triangular waveform, tests were conducted using two different procedures. In one test series, the temperature and R were held constant while the crack was grown for periods at various frequencies. In the other test category, while the frequency and temperature were held constant, the crack was grown for periods at different R values. Frequency and R sequences were selected to make distinct markings on the fracture surface. These marks were later used in verifying the crack lengths measured by d.c. potential and compliance methods. Figure 2 provides an example of a fracture surface from the tests. After fracture, each specimen was prepared for observation under optical and scanning electron microscope to determine the mechanisms of crack growth.

## 2.7 GROWTH RATE MONITORING

At the beginning of the test, the frequency and R sequence for the specimen was input to the computer. After each growth segment of 0.75 mm, either the frequency or R was automatically changed as specified. While the test was being conducted, the crack length as a function of the number of cycles was monitored by the operator on a graphical display. Crack growth rates derived from a linear regression representation of the data over the region where constant growth rate was observed were also displayed. With the aid of this real-time display of data, the

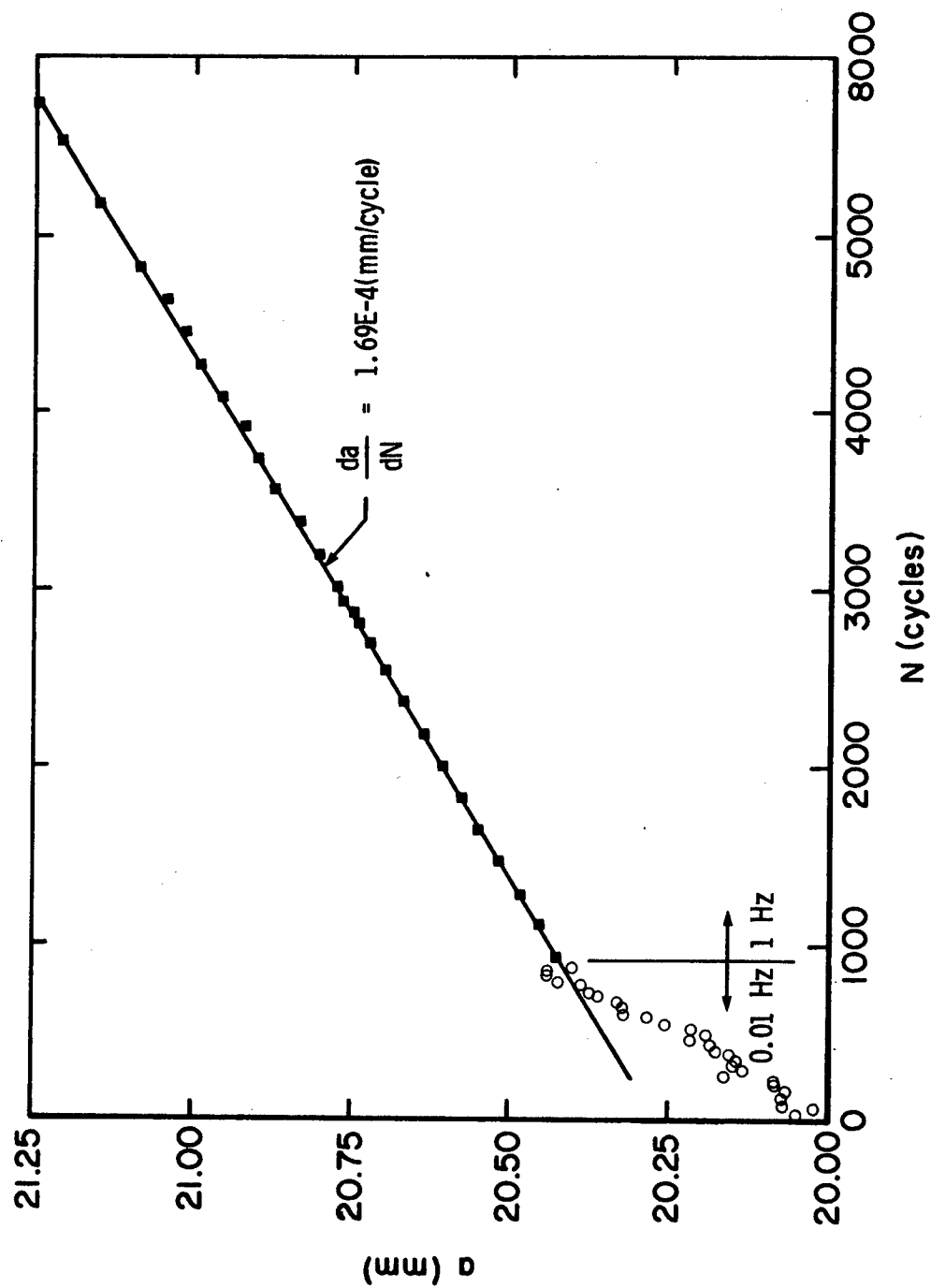


Figure 2. Fractured Specimens of Inconel 718 Showing Different Cracking Regions Corresponding to Test Under Different Conditions.

FCGR were obtained within crack extensions as small as 0.5 mm for given combinations of frequency, temperature, R, and  $K_{\max}$  values. The graphical display also helped the operator determine if the crack growth rate had reached a steady-state value. This sophisticated testing procedure made it possible to obtain large amounts of data within a short time with very few specimens. To check the variability of growth rate, the crack was grown at  $f = 1$  Hz,  $T = 650^{\circ}\text{C}$ ,  $R = 0.1$ , and  $K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$  at various crack lengths in the specimens. The variability of the FCGR from specimen to specimen and location to location was observed to be within a scatterband of 10% from the mean value for a given set of  $f$ ,  $R$ ,  $T$ , and  $K_{\max}$  [16].

### SECTION 3

#### RESULTS AND DISCUSSION

##### 3.1 GROWTH RATE-FREQUENCY PLOTS AT $R = 0.1$

Fatigue crack growth data were obtained for Inconel 718 alloy as a function of frequency at  $R = 0.1$  and at a temperature of  $650^{\circ}\text{C}$ . Typical crack length vs cycle data with a fitted linear line are shown in Figure 3 for a given test condition ( $K_{\text{max}} = 27.8 \text{ MPa}\cdot\text{m}^{1/2}$  and  $f = 1 \text{ Hz}$ ). FCGR data as a function of frequency, obtained by fitting a least square error linear regression line for the crack length versus cycles curves are shown in Figure 4 for the maximum stress intensity factors of 27.8 and  $40 \text{ MPa}\cdot\text{m}^{1/2}$  for  $R = 0.1$  and  $T = 650^{\circ}\text{C}$ . Also in this figure, FCGR data at 1 Hz in vacuum [17] at  $650^{\circ}\text{C}$ , and at 1 and 4 Hz in air at room temperature are given for both  $K_{\text{max}}$  values. In Figure 5, FCGR data for  $K_{\text{max}} = 40 \text{ MPa}\cdot\text{m}^{1/2}$  are presented using a time basis, i.e.,  $da/dt$  is described as a function of frequency.

In Figure 4, the  $da/dN$  versus frequency curves can be represented with three linear lines separated by frequencies  $f_{\text{tm}}$  and  $f_{\text{mt}}$ , with a continuous transition from one to the other. The curve representing  $K_{\text{max}} = 40 \text{ MPa}\cdot\text{m}^{1/2}$  is discussed in detail in the proceeding paragraphs.

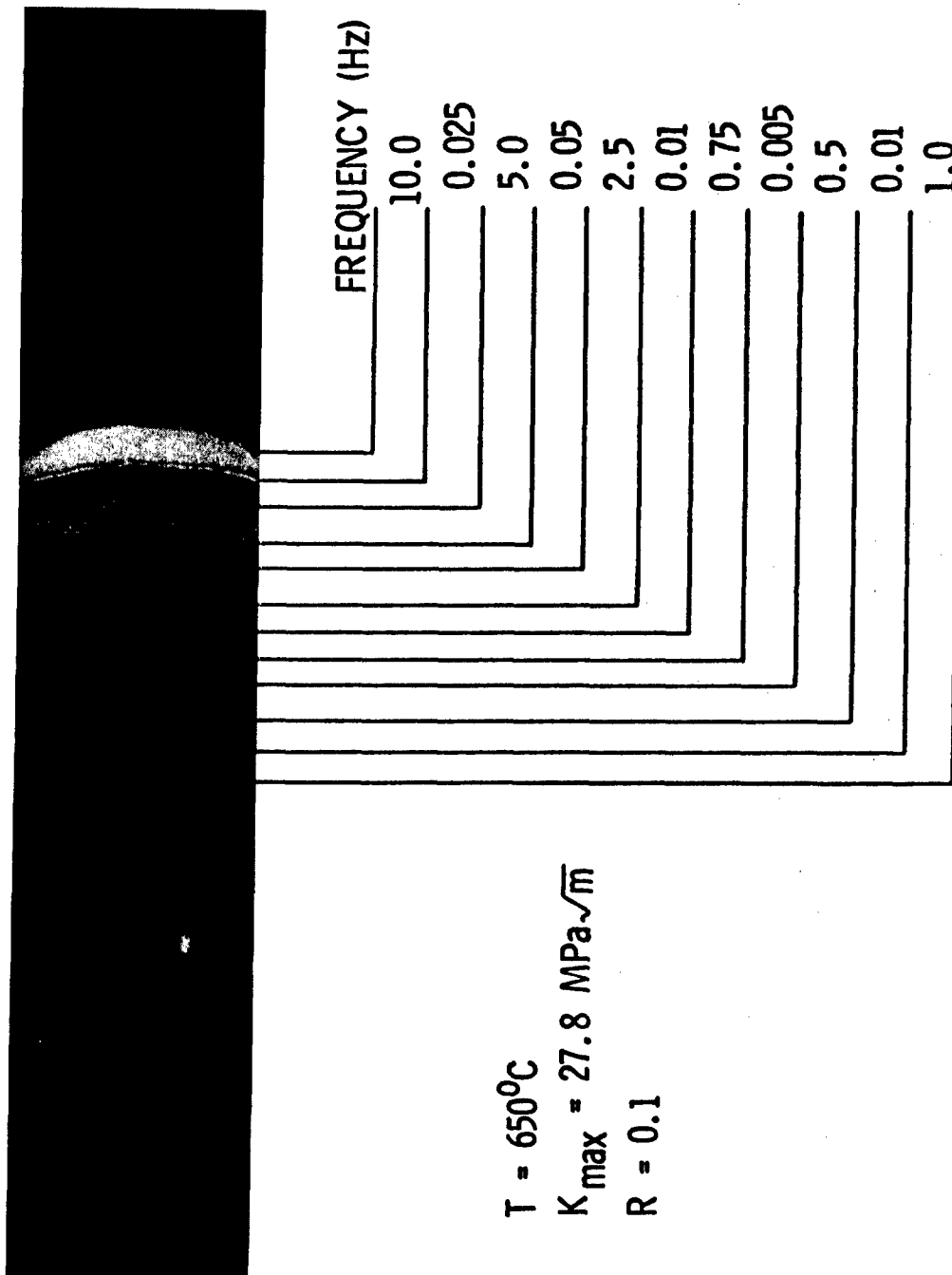


Figure 3. Typical  $a$  vs  $N$  Experimental Data with the Fitted Linear Regression Line.



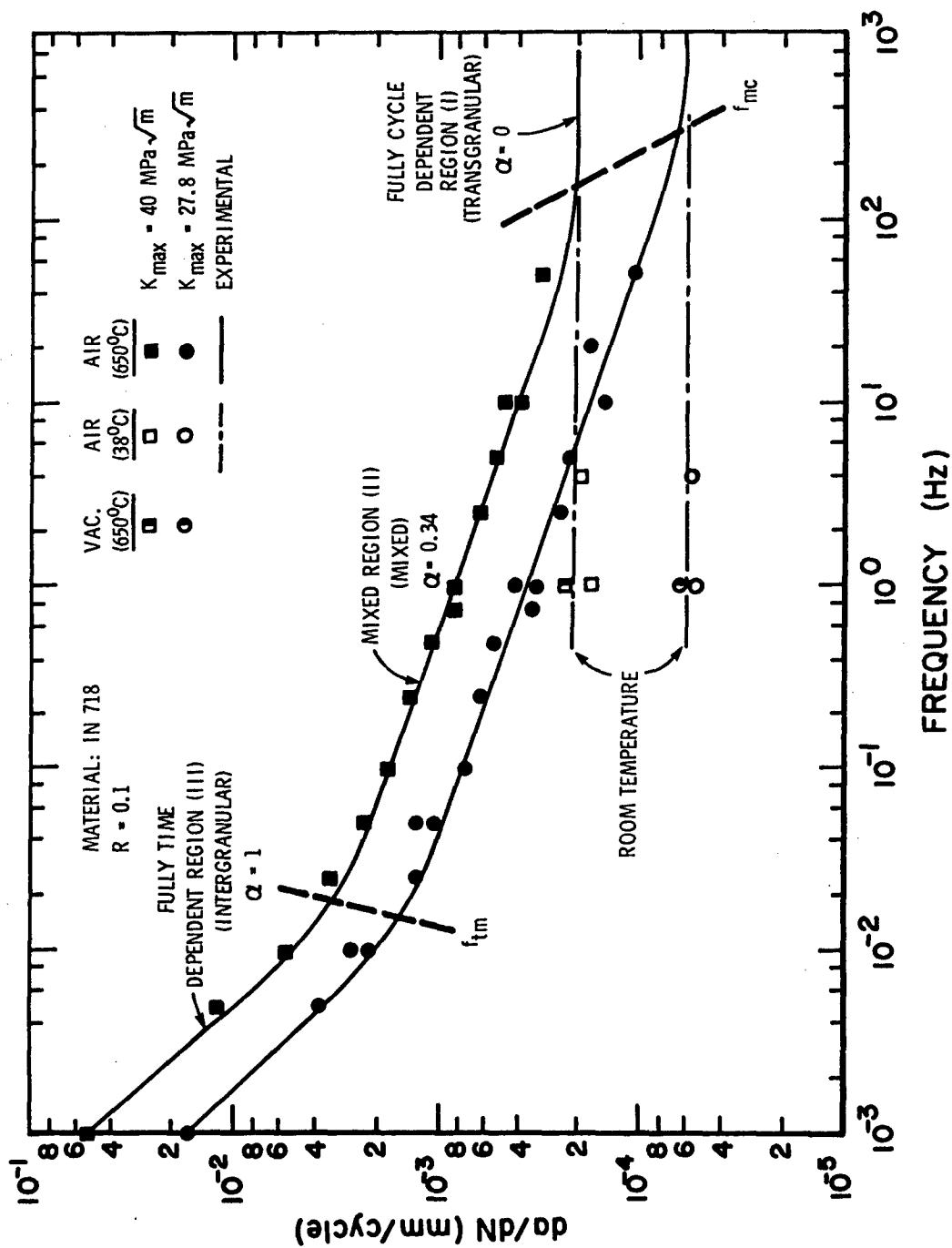


Figure 4. Fatigue Crack Growth Rate (da/dN) for Inconel 718 as a Function of Frequency at  $R = 0.1$ ; Temperature = 650°C at Two Different  $K_{max}$  Values, 27.8 and 40  $\text{MPa}\cdot\text{m}^{1/2}$ . Also Data in Vacuum at 1 Hz [17] and Room Temperature Air Data are Given.

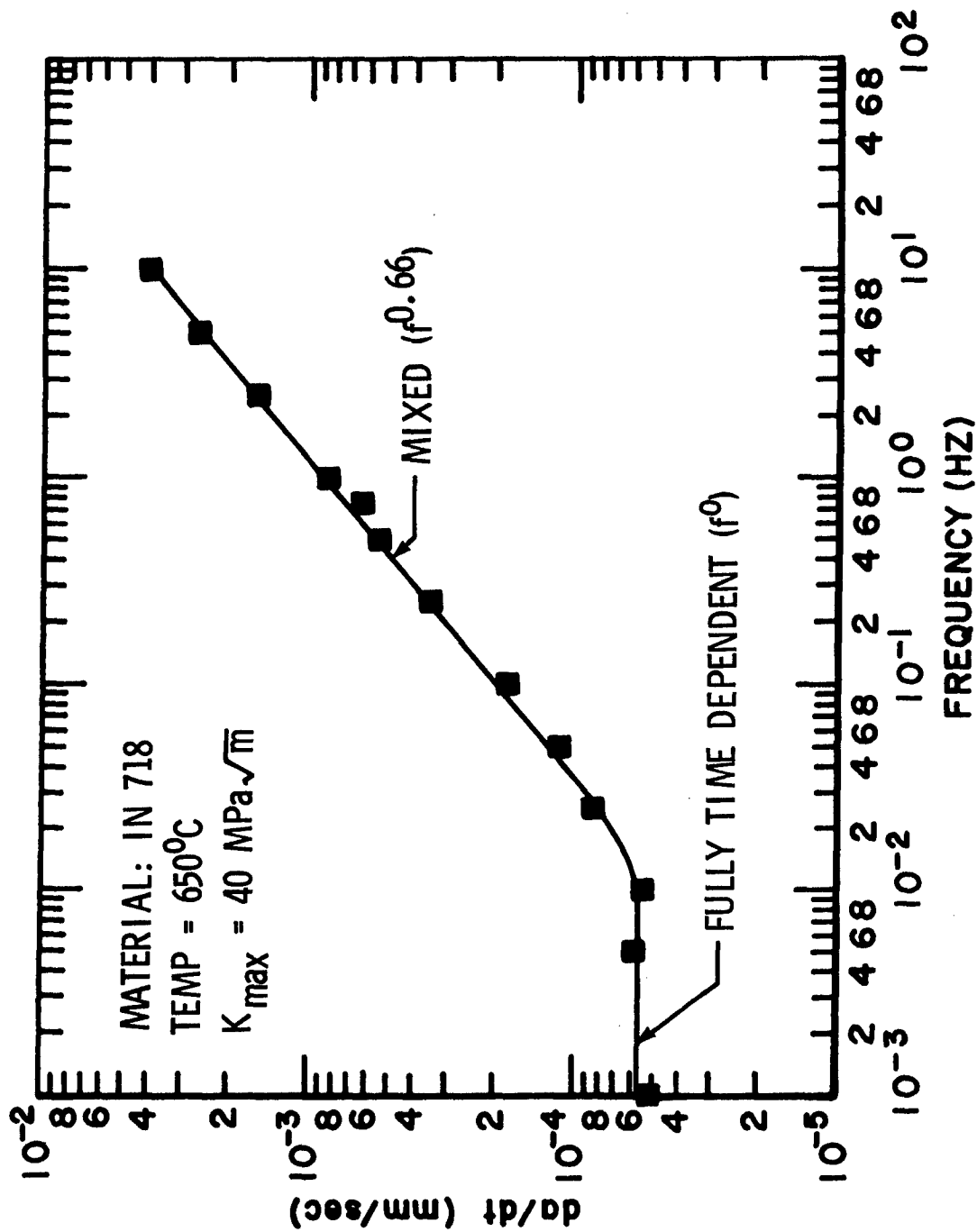


Figure 5. Time Rate of Crack Growth,  $(da/dt)$  for Inconel 718 as a Function of Frequency at  $K_{max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$ ,  $R = 0.1$ , and Temperature = 650°C.

### 3.1.1 Fully Time-Dependent Growth

In Figure 4, FCGR increases with decreasing frequency with a slope of -1 for the portion of the curve for frequencies below 0.01 Hz. This region represents fully time-dependent behavior where cycling has no effect on the growth rate based on time. The horizontal region of the  $da/dt$  curve in Figure 5 also illustrates the fact that the processes are fully time-dependent in this frequency regime. Under these conditions, time that is required to grow the crack a specific distance is a constant, and therefore, the factors determining the growth is independent of the number of cycles elapsed during that time. The damage is believed to occur by an environmentally enhanced rather than by a classical creep process.

### 3.1.2 Environmentally Enhanced Cycle-Dependent (Mixed) Growth

For frequency values between 0.01 and 10 Hz, log-log plots of  $da/dN$  versus frequency is linear with a slope of -0.34. In this middle frequency region, environment is affecting the cyclic damage and fracture is due to an environmentally enhanced fatigue process (mixed mode region).

### 3.1.3 Fully Cycle-Dependent Growth

Although there are not many data points at frequencies greater than 10 Hz for higher frequencies,  $da/dN$  is constant and should approach the frequency independent growth rate line at room temperature or high vacuum at 650°C. Though such a behavior was not specifically observed in air tests at 650°C, as we were unable to achieve ultra-high frequencies for the work reported in this paper, it was observed by Tien [18] that if the frequencies were sufficiently high, the effect of oxygen on the elevated temperature fatigue behavior could be suppressed resulting in a time-dependent but fully cycle-dependent process of damage. The asymptotic nature of the growth rate at higher frequencies was also proposed by Solomon and Coffin [11]. At frequencies greater than 50 Hz, fatigue crack growth is occurring so fast that there is insufficient time for environment to contribute to any damage at the crack tip. Hence, at very high frequencies, growth rates should approach the frequency independent growth rates at room temperature or in high vacuum at 650°C where there is no environmental damage. In this region, fracture at the crack tip is believed to occur under a pure cyclic plastic deformation process. In both cases, though there is no environmental damage at the crack tip due to oxidation, at room temperature, rewelding of the crack is prevented by the surface oxide film [19]. To establish the FCGR frequency behavior independent of environmental effects at 650°C, additional work is being conducted in vacuum [20].

### 3.2 EFFECT OF $K_{\max}$ ON FCGR-FREQUENCY PLOTS AT A GIVEN R (R = 0.1)

Fatigue crack growth rates as a function of frequency are shown in Figure 4 for maximum stress intensity factors of  $27.8 \text{ MPa}\cdot\text{m}^{1/2}$  and  $40 \text{ MPa}\cdot\text{m}^{1/2}$ . Both of the stress intensity values in Figure 4 lie in the mid-power law region of the  $da/dN$  versus  $K_{\max}$  curve as shown by Ashbaugh [9]. When  $K_{\max}$  is  $27.8 \text{ MPa}\cdot\text{m}^{1/2}$ , we also observed the existence of the above discussed three regions at  $650^\circ\text{C}$ . For the fully time-dependent region,  $da/dN$  is observed to be an inverse function of frequency,  $f$ , while for the mixed region, it is an inverse function of  $f^\alpha$  ( $\alpha = 0.34$ ). At very high frequencies, that is in the fully cycle-dependent region, growth rates should approach a constant value, the room temperature growth rate, which is independent of the frequency and hence, the oxidizing environment. The slopes of the three regions of the  $da/dN$  versus frequency curves are seen to be reasonably independent of  $K_{\max}$  for a given R value of 0.1 at  $650^\circ\text{C}$  for the two values of  $K_{\max}$  chosen in this investigation. Also from Figure 4, as  $K_{\max}$  increases, transition frequency from time-dependent to mixed regime increases and transition frequency from mixed to cycle-dependent decreases.

### 3.3 EFFECT OF R ON GROWTH RATE-FREQUENCY PLOTS AT

$$K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$$

Tests were conducted at  $K_{\max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$  for values of  $R = 0.1, 0.5, \text{ and } 0.8$ . The purpose of these tests was to examine the effect of stress ratio on FCGR as a function of frequency. Observed FCGR data are shown in Figure 6. Also data in vacuum [17] at 1 Hz and in air at 650°C and room temperature, respectively, are presented in this figure for  $R = 0.1$  and 0.5. At very high frequencies, FCGR is independent of frequency and should approach the growth rate at room temperature. All FCGR-frequency data in air at 650°C were characterized as falling within one of three regions: a fully time-dependent region with a slope of -1, a mixed region with a slope of -0.34, and a fully cycle-dependent region with a slope of zero. As  $R$  values were increased, the transition frequencies were shifted toward higher frequencies. Therefore, all three regions of crack growth were not observed for the high  $R$  values since some of the transition frequencies apparently fell outside the range of tested frequencies. In this study, for  $R = 0.5$ , only the fully time-dependent and mixed mode regions were observed. For  $R = 0.8$ , all data appeared to lie in the fully time-dependent region. For a given frequency, as  $R$  was increased, crack growth rate behavior tends to shift from a fully cycle-dependent mode to a mixed mode, and finally to a fully time-dependent mode. This behavior was expected since, as  $R$  was increased, the crack tip tends to be at

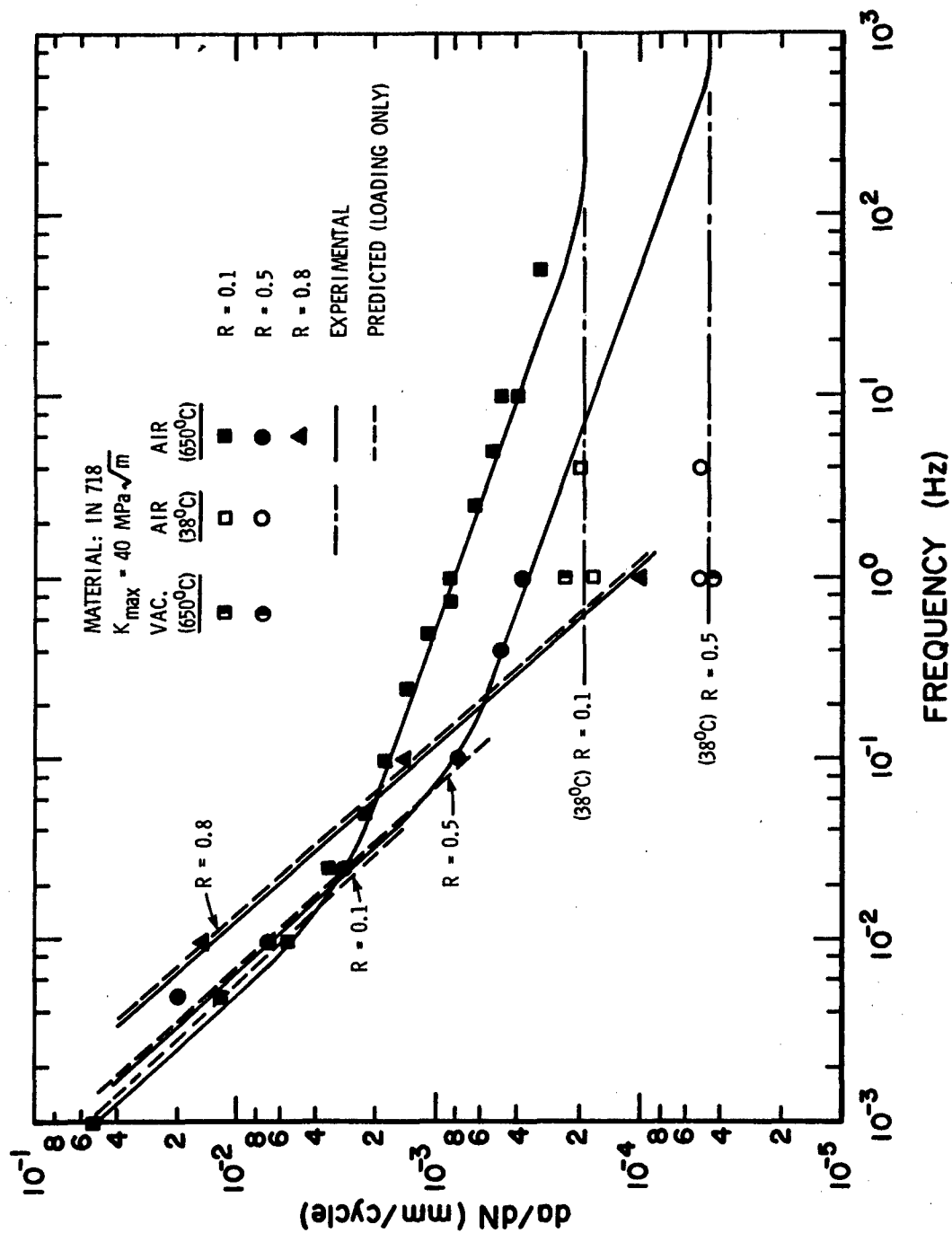


Figure 6. Fatigue Crack Growth Rate, (da/dN) for Inconel 718 as a Function of Frequency at  $K_{max} = 40 \text{ MPa}\cdot\text{m}^{1/2}$  and Temperature = 650°C for Three Different R Values, 0.1, 0.5, and 0.8. Also 1 Hz Vacuum Data Points [17] and Room Temperature Data are Given for R = 0.1 and 0.5.

higher loads for a longer time for the same frequency, thus promoting environmentally enhanced damage at the crack tip.

### 3.4 TRANSITION FREQUENCIES

From Figures 4 and 6, the existence of transition frequencies from fully time-dependent to mixed fracture ( $f_{tm}$ ), and from mixed fracture to fully cyclic-dependent fracture ( $f_{mc}$ ), can be observed. Using these transition frequencies at a constant temperature, Equation 1 can be written in the form

$$(da/dN)_T = F_c(R, K_{max}) \cdot f_{mc}^\alpha \cdot f_{tm}^{(1-\alpha)} \cdot [1/f] \cdot [1 + (f/f_{tm})^2]^{(1-\alpha)/2} [1 + (f/f_{mc})^2]^{\alpha/2} \quad (4)$$

where  $F_c(R, K_{max})$  is the fatigue crack growth rate as a function of  $K_{max}$  and  $R$  and room temperature and high frequency, and  $\alpha$  corresponds to the negative slope of the mixed region of the fatigue crack growth rate versus frequency curves. Fatigue crack growth maps such as shown in Figure 4 and given in Equation 4, can be used to indicate transition frequency boundaries and FCGR behavior of three regions of fatigue crack growth [21].

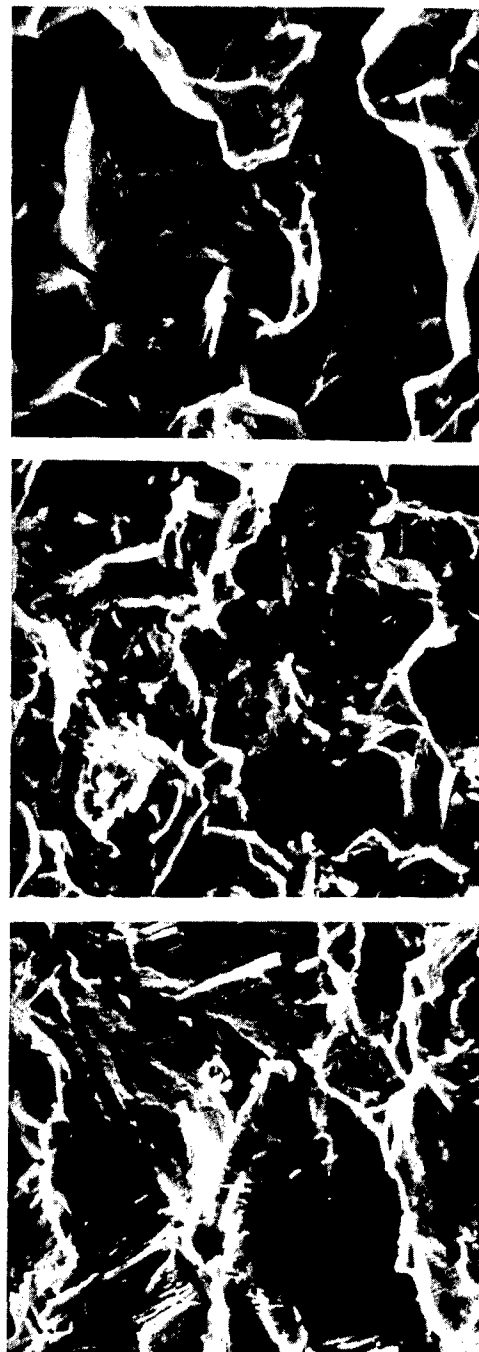
### 3.5 MICRO-MECHANISMS OF CRACK GROWTH

Figure 7 shows typical fractographs taken from the three frequency regimes discussed above. An example of the fully cycle-dependent region is shown in Figure 7a. As shown, crack



INCONEL 718  
 TEMPERATURE: 650°C  
 $K_{max} = 40 \text{ MPa}\sqrt{m}$

$\frac{4\mu}{1}$



(a)  $f = 10 \text{ Hz}$  (b)  $f = 0.5 \text{ Hz}$  (c)  $f = 0.001 \text{ Hz}$

Figure 7. Scanning Electron Fractographs of Typical Fracture Surfaces for (a) Cycle-Dependent (10 Hz) Region, (b) Mixed (0.5 Hz) Region, and (c) Time-Dependent (0.001 Hz) Region. These Tests Were Conducted at 650°C,  $R = 0.1$ , and  $K_{max} = 40 \text{ MPa}\cdot m^{1/2}$ .

growth is caused by the formation of striations due to cyclic plastic deformation at the crack tip. A typical fracture surface taken from the mixed mode region is given in Figure 7b. In this case, a mixture of transgranular and intergranular fracture was observed. Figure 7c is a typical representation of fracture in the fully time-dependent region. In this region, cracking occurred only along the grain boundaries, and the total fracture surface was covered with grain boundary facets.

In general, as frequency was decreased, fracture morphology changed from pure transgranular to a mixture of transgranular-intergranular and finally to a fully intergranular mode independent of frequency,  $R$ , or  $K_{\max}$ . These three frequency regimes that correspond to the observed changes in the fracture morphology are approximately identical to the regimes that were detected from the changes in the slopes of FCGR-frequency curves discussed in previous sections for different values of  $R$  as well as  $K_{\max}$  as shown in Figures 4 and 6.

### 3.6 MECHANISMS OF DAMAGE IN FULLY TIME-DEPENDENT REGIME

In the time-dependent region, crack growth occurred along the grain boundaries. Among the factors that could account for the time-dependent mechanisms are oxidation damage and creep-fatigue damage along the grain boundaries. Creep damage normally occurs by grain boundary cavitation and triple point cracking [22,23]. There was very little evidence of the presence of

either of these mechanisms. Thus, the environment appears to dominate the mechanism for damage under time-dependent conditions. There is evidence for this type of damage on the fracture surfaces; cracks were covered with oxides at lower frequencies. In general, oxygen can diffuse through grain boundaries faster than the bulk material at high temperatures. Environmental embrittlement of nickel-base superalloys at high temperature by oxygen penetration along the grain boundaries has been postulated in detail by Woodford and Bricknell [24]. In nickel-base superalloys, embrittlement is due to the penetration of gaseous species, primarily oxygen along the grain boundaries. Oxidation kinetics along the grain boundaries can be represented by an expression of the form

$$d = C \cdot t^n \cdot \exp(-Q/RT) \quad (5)$$

where  $d$  is the depth of oxygen penetration,  $C$ ,  $n$ ,  $Q$ , and  $R$  are constants,  $T$  is temperature, and  $t$  is time [25]. But Equation 5 may not be applicable in modeling the grain boundary oxidation kinetics because the stress effects are not represented in the expression.

### 3.7 MODELING THE GROWTH BEHAVIOR

Phenomena of corrosion fatigue crack growth rate behavior (two regimes of pure cycle- and pure time-dependency in these cases) have been described in terms of linear superposition by

Gallagher and Wei [26], and Solomon and Coffin [11] for low cycle fatigue crack growth in vacuum at high temperature. As Solomon [10] has seen, crack growth rate data could not be expressed with a linear superposition model when the mixed regime is appreciably large. From Figures 4 and 6, FCGR at 650°C for a  $K_{max}$  in the mid-power law region of growth rate behavior and R values up to a maximum of 0.8 can be represented by the general expression

$$da/dN = \text{MAX}(F_c, F_m, F_t) \quad (6)$$

where  $F_c$ ,  $F_m$ , and  $F_t$  are functions of R, f, and  $K_{max}$  which describe the FCGR behavior in the three frequency regimes, cycle-dependent, mixed, and time-dependent, respectively. In Equation 6, MAX function represents the maximum value of  $F_c$ ,  $F_m$ , and  $F_t$ . The unified expression given in Equation 6 can be easily incorporated into a computer life prediction scheme, as almost all computer compilers have a built-in intrinsic MAX function. Separate prediction procedures of the above three functional expressions are discussed below.

### 3.7.1 Prediction of Growth Rates in the Fully Time-Dependent Region

A prediction was made of the cyclic crack growth rate under fully time-dependent behavior based solely on sustained load crack growth data. For this case, by integrating

the sustained load crack growth behavior during the total time period of the triangular waveform,

$$\frac{da}{dN} = 2 \int_0^{\frac{1}{2}f} \frac{da}{dt} s \cdot dt = 2C \int_0^{\frac{1}{2}f} [K(t)]^n \cdot dt \quad (7)$$

where  $K(t)$  varies linearly with time for the triangular waveform and given by

$$K(t) = R \cdot K_{\max} + 2 \cdot K_{\max} \cdot (1-R) \cdot t \cdot f \quad (8)$$

$f$  is the frequency, and  $da_s/dt = C \cdot K^n$  is the sustained load crack growth behavior of the material ( $n = 3$ ). In Equation 7,  $da/dN$  represents the crack growth in one cycle. From substituting the triangular waveform relation for  $K(t)$  in Equation 7,

$$\frac{da}{dN} = \frac{C \cdot K_{\max}^n}{f} \cdot \frac{[1-R^{n+1}]}{(n+1)(1-R)} \quad (9)$$

For the triangular waveform in the fully time-dependent region, the crack growth rates predicted by Equation 9 were approximately two times that of experimental data for a given frequency. Hence, for the triangular waveform in the fully time-dependent region, as shown in Figure 6, crack growth rate could be predicted by integrating the sustained load crack growth behavior along only the rising portion of the cycle. Dashed lines represent the predicted data from Equation 7 integrating only on the loading cycle of the waveform. This is consistent with the observations by Ashbaugh [9] who showed that under non-symmetric waveshape loading, the observed FCGR corresponds to

FCGR of the rising portion of the cycle only. But as  $R$  increases above 0.8, the cycling driving force,  $\Delta K$  will be less than  $\Delta K_{th}$  for this material. Assuming when  $R > 0.8$  that the integration should be performed on the total period of the cycle, FCGR in the fully time-dependent regime is given by the expression

$$F_t(R, K_{max}, f) = \frac{da}{dN} = \frac{C \cdot K_{max}^n}{f} \cdot \frac{[1-R^{n+1}]}{(n+1)(1-R)} \cdot y \quad (10)$$

where  $y = 0.5$  for  $(1-R)K_{max} \geq \Delta K_{th}$ , and  $y = 1.0$  for  $(1-R)K_{max} < \Delta K_{th}$ . An expression of this type would satisfy the limit condition,  $R \rightarrow 1$ , where  $(da/dN) \cdot f$  should approach the sustained load crack growth rate,  $da/dt$ .

### 3.7.2 Prediction of Growth Rates in the Mixed Region

In the mixed region, FCGR was shown above to be proportional to  $f^{-\alpha}$  for  $R = 0.1$  and  $0.5$  at  $K_{max}$  of  $40 \text{ MPa} \cdot \text{m}^{1/2}$ , and for  $R = 0.1$  at  $K_{max}$  of  $27.8 \text{ MPa} \cdot \text{m}^{1/2}$ . Using this observation, FCGR can be represented by the expression

$$F_m(R, K_{max}, f) = da/dN = C_m \cdot R_m(R) \cdot (K_{max}^{nm}/f^\alpha) \quad (11)$$

where  $C_m$  and  $nm$  are constants, and  $R_m$  is a function of  $R$ . If  $R_m$  is assumed to be of the Walker form [27,28]

$$R_m(R) = (1-R)^{mm} \quad (12)$$

then mm could be evaluated from the data given in Figure 6 (mm = 1.50 and nm = 2.42). We were unable to verify this expression from the study reported in this report, as only two data points (R = 0.1 and 0.5) were available for any frequency chosen from the mixed regime. In future work, additional experiments will be conducted at other R values between 0.1 and 0.5 for more data points in this regime.

### 3.7.3 Prediction of Growth Rates in Fully Cycle-Dependent Region

In the fully cycle-dependent or environmentally-independent regime, FCGR is independent of the frequency. Also in this regime, the FCGR approaches a value given by a room temperature experiment as discussed earlier. Figure 8 shows the FCGR as a function of (1-R) for two  $K_{max}$  values, 27.8 and 40 MPa·m<sup>1/2</sup> at room temperature. In this log-log plot, the variation of FCGR can be represented by straight lines for both  $K_{max}$  values where slopes of the two lines (mc) are identical, and mc = 2.14. In this frequency regime, FCGR can be represented by the expression

$$F_c(R, K_{max}) = da/dN = Cc \cdot (1-R)^{mc} \cdot K_{max}^{nc} \quad (13)$$

where nc = 3.04.

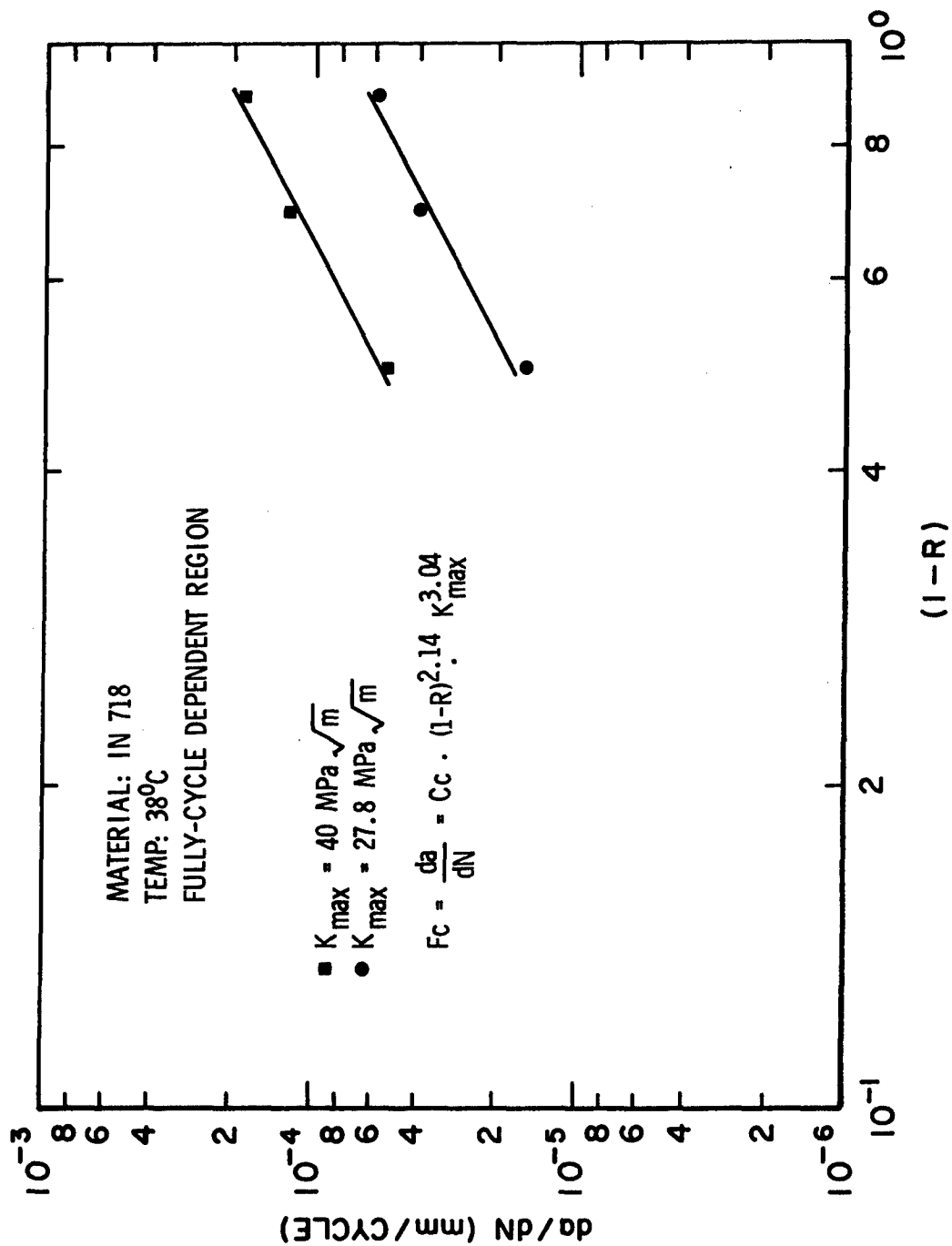


Figure 8. FCGR for Inconel 718 at Room Temperature (38°C) and 1 Hz as a Function of  $(1-R)$  for  $K_{\max} = 27.8$  and  $40 \text{ MPa}\cdot\text{m}^{1/2}$ .



## SECTION 4

### CONCLUSIONS

At high temperatures, frequency dependence of fatigue crack growth rate can be divided into three modes of damage: fully cycle-dependent, mixed, and fully time-dependent damage, irrespective of  $R$  values, maximum stress intensity, and frequency. Three different models were derived for these frequency regimes which can be represented with a single function to get the overall crack growth rate under any condition of  $R$ ,  $K_{max}$  (in the mid-power law regime) and frequency as shown in Equation 6. Micro-mechanisms of fatigue crack growth which were obtained from extensive fracture surface analysis also indicate the existence of these three regimes of damage, thus providing a physical basis for the above modeling.

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